The CyCab: a car-like robot navigating autonomously and safely among pedestrians

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Received 1 November 2003; received in revised form 11 October 2004; accepted 12 October 2004

Available online 25 December 2004

Abstract

The recent development of a new kind of public transportation system relies on a particular double-steering kinematic structure enhancing manoeuvrability in cluttered environments such as downtown areas. We call bi-steerable car a vehicle showing this kind of kinematics. Endowed with autonomy capacities, the bi-steerable car ought to combine suitably and safely a set of abilities: simultaneous localisation and environment modelling, motion planning and motion execution amidst moderately dynamic obstacles. In this paper we address the integration of these four essential autonomy abilities into a single application. Specifically, we aim at reactive execution of planned motion. We address the fusion of controls issued from the control law and the obstacle avoidance module using probabilistic techniques.

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Keywords: Car-like robot; Navigation; Path planning; Obstacle avoidance; Autonomous navigation

1. Introduction

The development of new intelligent transportation systems (ITS), more practical, safe and accounting for environmental concerns, is a technological issue of highly urbanised societies today [18]. One of the long run objectives is to reduce the use of the private automobile in downtown areas, by offering new modern and convenient public transportation systems. Examples of these are the CyCab robot—designed at INRIA and currently traded by the Robosoft company (see http://www.robosoft.fr)—and the pi-Car prototype of IEF (Institut d’Electronique Fondamentale, Université Paris-Sud).

The kinematic structure of these robots differs from that of a car-like vehicle in that it allows the steering of
both the front axle and the rear one. We call a vehicle showing this feature a bi-steerable car (or BiS-car for short).

Endowed with autonomy capacities, the bi-steerable car ought to combine suitably and safely a set of abilities that eventually could come to the relief of the end-user in complex tasks (e.g. parking the vehicle). Part of these abilities have been tackled separately in previous work: simultaneous localisation and environment modelling, motion planning execution amidst static obstacles and obstacle avoidance in a moderately dynamic environment without accounting for a planned motion.

In this paper we address the integration of these four essential autonomy abilities into a single application. Specifically, we aim at reactive execution of planned motion. We address the fusion of controls issued from the control law and the obstacle avoidance module using probabilistic techniques. We are convinced that these results represent a step further towards the motion autonomy of this kind of transportation system.

The structure of the paper is as follows. In Section 2, we sketch the environment reconstruction and localisation methods we used and we recall how the central issue regarding the motion planning and execution problem for the general BiS-car was solved. Section 3 explains how our obstacle avoidance system was designed and Section 4 explains how it was adapted to the trajectory tracking system. In Section 5 we present the experimental settings showing the fusion of these essential autonomy capacities in our bi-steerable platform the CyCab robot. We close the paper with some concluding remarks and guidelines on future work in Section 6.

2. Localisation, environment modelling, motion planning and execution

In the design of an autonomous car-like robot, we are convinced that localisation, modelling of the environment, path planning and trajectory tracking are of fundamental importance.

2.1. Map-building and localisation

The CyCab robot is the size of a golf-cab capable of attaining up to 30 km/h. Its “natural” environment is the car-park area of the INRIA Rhône-Alpes (about 10,000 m²). For localisation purposes, we did not want to focus on the detection of natural features in the environment, since such detection is often subject to failure and not very accurate. So, in order to ensure reliability, we decided to install artificial landmarks in the environment. These landmarks had to be detected easily and accurately, and they should be identified with a reasonable computation effort. Figs. 1 and 2 show our robot, its sensor and the landmarks: cylinder covered with reflector sheets, specially designed for our Sick laser range finder.

Moreover, in order to keep flexibility, we wanted to be able to equip the environment with non-permanent beacons. For this reason, we could not rely on a definitive landmark map, and we had to build a system able to learn the current state of the car-park area. This led us to use SLAM methods. The method which was the best suited to our needs was the geometric projection filter (see [21] for reference, and [24] for implementation details). It consists in building a map of features uncorrelated with the robot state. Such features are, for instance, the distance between landmarks or angles between three of them.

Owing to the accuracy of the laser range finder, to the good choice of our landmarks, and to the strength of the SLAM methods we use, we evaluate the worst case accuracy of our localisation system to the following value: about 10 cm in position and 2° in orientation.

We refer the reader to [24] for more details about the way we evaluate these values.

2.2. The obstacle map

The previous method localises the robot and builds a landmark map. But, we still miss a map of observed obstacles in order to plan safe paths. To achieve this goal, we build a kind of simplified occupancy grid [8] on the environment. This structure gives us information correlated with the probability that a given place is the boundary of an obstacle.

Both maps are built online, in real-time, by the robot during the construction phase. Fig. 1 shows how the obstacle map evolves while we are exploring the environment. This map is made of small patches which are added according to the need of the application.
2.3. Motion planning amidst static obstacles

The motion planner adopted for the CyCab was presented in [26]. Essentially, it is a two-step approach, dealing separately with the physical constraints (the obstacles) and with the kinematic constraints (the non-holonomy). The planner first builds a collision-free path without taking into account the non-holonomic constraints of the system. Then, this path is approximated by a sequence of collision-free feasible sub-paths computed by a suitable\textsuperscript{2} steering method. Finally, the resulting path is smoothed.

A key issue in non-holonomic motion planning is to find a steering method accounting for the kinematics of the robot. One way of designing steering methods for a non-holonomic system is to use its flatness property as explained in [26].

\textsuperscript{2} That is, verifying the topological property as explained in [26].
Fig. 3. CyCab robot, its landmarks and its kinematics model showing the coordinates of the flat output (point $H$) with respect to the reference frame of the robot placed at point $F$. In our case we have that $(x_F, y_F, \theta, \phi)$ is the state of the robot.

Fig. 4. Path computed by the motion planner using a real obstacle map. The obstacles are grown as well as the robot before computing the path.

The interface is used to display the current position of the robot within its environment and capture the goal position entered by the user. These positions together with the obstacle map are passed to the motion planner. The output path is then displayed allowing the user to validate the path or start a new search.

Finally, the reference trajectory is generated using a regular parameterisation of the path [16] and the user is requested to accept to start the execution of the trajectory.

2.4. Steering a BiS-car

The kinematics model of a general bi-steerable vehicle and its flat output are shown in Fig. 3.

The striking advantage of planning a path in the flat space is that we only need to parameterise a two-dimensional curve whose points and derivatives define everywhere the current $n$-dimensional state of the robot (in the case of the BiS-car $n = 4$). The main characteristic of such a curve is its curvature $\kappa$ from which the steering angle can be computed.

Fig. 4 shows the outcome of the motion planner using an obstacle map generated as described in the previous section.

2.5. User–planner interface

The user–planner interface in the CyCab is achieved through a touch-screen superposed to a 640 x 480 pixels LCD display. Additionally, we use the keyboard to allow for the entrance of data.

The configuration space in robotics is called the state space in control theory, so we will use indistinctly both terms.

2.6. Trajectory tracking using flatness

It is well known that a non-holonomic system cannot be stabilised using only smooth state static feedbacks [6]. Ever since then, time-varying feedbacks [25] and dynamic feedbacks have been successfully used in particular for the canonical tractor-trailer and car-like robots [9].

Flat systems are feedback linearisable by means of a restricted class of dynamic feedback called endogenous [10]. The interest is that we are able to use state-of-the-art linear control techniques to stabilise the system.

We present here results coming from recent work on feedback linearisation of the general BiS-car.

For a reference frame of the robot placed at point $F$ in Fig. 3, the flat output $y = (y_1, y_2)^T$ of a BiS-car are the coordinates of a point $H = (x_H, y_H)^T = (y_1, y_2)^T$. The configurations of the robot are linearised around this point.
Computed as a function of the state as follows:

\[ H = F + P(\theta) \dot{\theta}u_\theta + Q(\theta) \dot{\theta}u_{\perp} \]

where \( P(\theta) \) and \( Q(\theta) \) are the coordinate functions relative to the robot’s reference frame (see [26] for details) and where \( \dot{\theta}_a \) (resp. \( u_{\perp} \)) are the unitary vector in the direction \( \theta \) (resp. the direction \( \theta + \pi/2 \)).

Looking for a tractable relation between the controls of the robot and the linearising output, we found an expression giving the flat output dynamics with respect to a more convenient reference frame placed at the middle of the front axle of the robot (point \( P \)) and having orientation \( \gamma = (\theta + \beta(\phi)) \pm \pi \) where the function \( \beta(\phi) \) is the characteristic angle of the velocity vector of the flat output.

The convenience of this new reference frame relies on the fact that the velocity of the flat output has a single component in it. More precisely—assuming that \( \gamma = \theta + \beta(\phi) + \pi \)—one can show that, in this reference frame, the flat output dynamics is given by the following expression [14]:

\[ \frac{\partial H}{\partial x} = v_\theta \dot{\theta}, \]

\[ v_\theta = v_\theta [\cos(\phi - \beta - \pi) - QJ + \omega_\phi \left( \frac{\partial P}{\partial \phi} - \frac{\partial Q}{\partial \phi} \right)], \]

\[ J(\phi) = \sin(\psi - f(\phi)) \]

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where \((v_\theta, \omega_\phi)\) are the controls of the robot (i.e. the heading and the front-steering speeds), \((\phi - \beta - \pi)\) the angle subtended between the velocity vector of the robot \( V_r \) and the velocity vector of the flat output \( V_H \) (see Fig. 3).

From expression (1) the open-loop controls of the robot can be found as soon as the trajectory of point \( H \) is known. As we are interested in stabilising the BiSscar around a reference trajectory, we explored the fact that, owing to the flatness property, the system is diffeomorphic to a linear controllable one [10]. The endogenous dynamic feedback that linearises the general bi-steerable system is presented in [14]. Then, from linear control theory, it can be shown that the closed-loop control stabilising the reference trajectory \( \gamma^* \) has the following form:

\[ \gamma^{(s)} = (\gamma^*_{y^{(s)}}) - \sum_{j=2}^{2} k_{y, j} \left( \gamma_{y^{(s)}} - (\gamma^*_{y^{(s)}}) \right), \quad i = 1, 2, \]  

\[ \text{where } (\gamma^{(s)}) \text{ stands for the total derivative of order } p. \]  


3. Obstacle avoidance using probabilistic reasoning

The previous approach considers trajectories in a static environment. In order to make the execution of these trajectories more robust, an obstacle avoidance system should be prepared to react to unpredicted changes in the environment. This section presents the principles of our obstacle avoidance module.

3.1. State of the art on reactive trajectory tracking

Most of the approaches for obstacle avoidance are local [11,5], that is they do not try to model the whole environment. Their goal is rather to use sensor measures to deduce secure commands. Being simpler and less computationally intensive, they seem more appropriate to fast reactions in a non-static environment. On the other hand, we cannot expect optimal solutions from a local method. It is possible that some peculiar obstacle configuration create a dead-end from which the robot cannot escape with obstacle avoidance only.

3.1.1. Potential fields

The general idea of potential fields methods, proposed initially by O. Khatib in 1986, is to build a function representing both the navigation goals and the need for obstacle avoidance. This function is built so as to decrease when going closer to the goal and increase near obstacles. Then, the navigation problems are reduced to an optimisation problem, that is, to find the commands that brings the robot to the global minimum of the function. This later can be defined with respect to the goal and the obstacles but other constraints can also be added therein.

Numerous extensions to the potential fields have been proposed since 1986. Among others, we can cite the virtual force fields [3], the vector field histograms...
Basically, these methods try to find the best path to the goal among the secure ones.

3.1.2. Steering angle field (SAF)

The SAF method, proposed by Feiten et al. in 1994, uses obstacles to constrain steering angle in a continuous domain. Simultaneously, speed control is an iterative negotiation process between the high-level driving module and the local obstacle-avoidance module. One of the first extension to this method was published in [27]. It expresses the collision avoidance problem as an optimisation problem in the robot controls space (linear and rotational speeds).

3.1.3. Dynamic window

The dynamic window approach [11] proposes to avoid obstacles by exploring command space in order to maximise an objective function. This later accounts for the progression toward the goal, the position of closer obstacles and current robot controls. Being directly derived from the robot dynamic, this method is particularly well adapted to high speed movements. The computational cost of the optimisation process is reduced using the dynamic characteristics of the robot (bounded linear and angular acceleration) so as to reduce the searched space. This kind of constraints are called hard constraints since the must be respected. Conversely, when the objective function includes preferences on the robot movement, we call the resulting constraints soft constraints.

3.1.4. Dynamic environments and velocity obstacles

In the specific case of moving obstacles, special methods have been proposed [17,2] using the velocity obstacle notion. Basically, this notion consists in projecting perceived obstacles and their expected movement in the space of secure commands. So, each mobile object generates a set of obstacles in the command space. These obstacles represent the commands that will bring to a collision in the future.

In the general case, obstacle movement parameters are not known a priori, so they have to be deduced from sensor data. Obstacle avoidance controls are then computed in reaction to these observations. Currently, it is still quite difficult to get reliable predictions of the obstacles future trajectory. Consequently, these obstacle avoidance methods are not applicable in real situations yet.

3.1.5. Obstacle avoidance and trajectory following

When we want to perform obstacle avoidance manoeuvres while following a trajectory, a specific problem appears. On our non-holonomous robot, the path planning stage took into account the kinematic of the robot and planned a feasible path. When the reactive obstacle avoidance generates commands, the vehicle leaves its planned trajectory. Then, we cannot be sure anymore that the initial objective of the trajectory is still reachable.

A solution to this problem was proposed in [20]. This method tries to deform the global trajectory in order to avoid the obstacle, respect the kinematic constraints and ensure that the final goal is still reachable. Even if theoretically very interesting, this obstacle avoidance scheme is still difficult to apply in real situations due to its computational complexities, especially on an autonomous car. In our experiments [20], the vehicle had to stop for several minutes in order to perform the trajectory deformation.

3.2. Objectives

After all these results on obstacle avoidance, it seems obvious that our goal is not to propose a new solution to this problem. It has been shown [19,1] that probabilities and Bayesian inference are appropriate tools to deal with real world uncertainty and model reactive behaviours. With this in mind, we wanted to think about the expression of the obstacle avoidance problem as a Bayesian inference problem. Consequently, the originality of our approach is mainly its expression and the semantic we can express with it.

3.3. Specification

The CyCab can be commanded through a speed $V$ and a steering angle $\Phi$. It is equipped with $\pi$ radians sweeping laser range finder. In order to limit the volume of the data we manipulate, we summarised the sensor output as eight values: the distances to the nearest obstacle in a $\pi/8$ angular sector (see Fig. 5). We will call
Fig. 5. Obstacle avoidance: situation.

$D_k, k = 1, \ldots, 8$ the probabilistic variables corresponding to these measures.

Besides, we will assume that this robot is commanded by some high-level system (trajectory following for instance) which provides it with a pair of desired commands ($V_d, \Phi_d$).

Our goal is to find commands to apply to the robot, guaranteeing the vehicle security while following the desired command as much as possible.

3.4. Sub-models definition

Given the distance $D_i$ measured in an angular sector, we want to express a command to apply that is safe while tracking desired command. Nevertheless, since this sector only has limited information about robot surrounding, we choose to express the following conservative semantic: tracking the desired command should be a soft constraint whereas an obstacle avoidance command should be a hard constraint, the closer is the obstacle, the harder is the constraint.

We express this semantic using a probability distribution over the commands to apply ($V, \Phi$) knowing the desired commands and the distance $D_i$ measured in this sector:

$$P_i(V | V_d D_i) = P_i(V | V_d D_i) P_i(\Phi | \Phi_d D_i),$$

(3)

where $P_i(V | V_d D_i)$ and $P_i(\Phi | \Phi_d D_i)$ are the Gaussian distributions, respectively, centred on $\mu_V(V_d, D_i)$ and $\mu_\Phi(\Phi_d, D_i)$ with standard deviation $\sigma_V(V_d, D_i)$ and $\sigma_\Phi(\Phi_d, D_i)$. Functions $\mu_V$, $\mu_\Phi$, $\sigma_V$, $\sigma_\Phi$ are defined with sigmoid shape as illustrated in Fig. 6. The examples of resulting distributions are shown in Fig. 7.

There are two specific aspects to notice in Figs. 6 and 7. First, concerning the means $\mu_V$ and $\mu_\Phi$, we can see that, the farther is the obstacle, the closer to the desired command $\mu$ will be, and conversely, the

Fig. 6. Evolution of mean and standard deviation of $P_i(V | V_d D_i)$ and $P_i(\Phi | \Phi_d D_i)$ according to distance measured.
nearer is the obstacle, the more secure is \( \mu \): minimal speed, strong steering angle.

Second, the standard deviation can be seen as a constraint level. For instance, when an obstacle is very close to the robot (small \( D_i \)), its speed must be strongly constrained to zero, this is expressed by a small standard deviation. Conversely, when obstacle is far, robot speed can follow the desired command, but there is no damage risk in not applying exactly this command. This low level constraint is the result of a big standard deviation.

3.5. Command fusion

Knowing desired controls and distance to the nearest obstacle in its sector, each sub-model, defined by \( P_i(V, \Phi | V_d, \Phi_d, D_i) \), provides us with a probability distribution over the robot controls. As we have eight sectors, we will have to fuse the controls from eight sub-models. Then we will find the best control in terms of security and desired control following.

To this end, we define the following joint distribution:

\[
P(V, \Phi | V_d, \Phi_d, D_1, \ldots, D_8) = P(D_1, \ldots, D_8) P(V|V_d, \Phi_d) P(S)
\]

(4)

where variable \( S \in \{1, \ldots, 8\} \) express which sector is considered. \( P(D_1, \ldots, D_8) \) and \( P(V|V_d, \Phi_d) \) are unknown distribution.\(^4\) As there is no need to favour a specific sub-model, we define \( P(S) \) as a uniform distribution. The semantic of \( S \) will be emphasised by the definition of \( P(V|V_d, \Phi_d, D_1, \ldots, D_8) \):

\[
P(V|V_d, \Phi_d, D_1, \ldots, D_8(S = i)) = P_i(V|V_d, \Phi_d, D_i).
\]

In this equation, we can see that the variable \( S \) acts as model selector: given its value \( i \), the distribution over the commands will be computed by the sub-model \( i \), taking into account only distance \( D_i \).

Using Eq. (4), we can now express the distribution we are really interested in, that is the distribution over the commands accounting for all the distances but not variable \( S \):

\[
P(V, \Phi | V_d, \Phi_d, D_1, \ldots, D_8) = \sum_{S} P(S) P(V|V_d, \Phi_d, D_1, \ldots, D_8(S)).
\]

(5)

This equation is actually the place where the different constraint level expressed by functions \( \sigma_v \) and \( \sigma_\Phi \) will be useful. The more security constraints there will be, the more peaked will be the sub-model control distribution. So sub-models who see no obstacles in their sector will contribute to the sum with quasi-flat distribution, and those who see perilous obstacles will add a peaky distribution, hence having more influence (see Fig. 8). Finally the command really executed by the robot is the one which maximise \( P(V, \Phi | V_d, \Phi_d, D_1, \ldots, D_8) \) (Eq. (5)).

3.6. Results

Fig. 9 illustrates the result of the obstacle avoidance system applied on a simulated example. The simulated CyCab is driven manually with a joystick in a square

\(^4\) Actually, as we know we will not need them in future computation, we do not have to specify them.
environment. In this specific situation, the driver is continuously asking for maximum speed, straightforward (null steering angle). We can observe on the dotted trajectory that, first obstacle avoidance module bends the trajectory in order to avoid the walls, and second, when there is no danger of collisions, desired commands are applied exactly as requested.

From the density of dots, we can figure out the robot speed: it breaks when it comes close to the walls and while its turning and try to follow desired speed when obstacles are not so threatening.

3.7. Relation to fuzzy logic approaches

The design of our obstacle avoidance modules may remind some readers of a fuzzy logic controller [15,22,12]. It is rather difficult to say that one approach is better than the other. Both fuzzy logic and Bayesian inference view themselves as extension of classical logic. Furthermore, both methods will deal with the same kind of problems, providing the same kind of solutions. Some will prefer the great freedom of fuzzy logic modelling and others will prefer to rely on the
strong mathematical background behind Bayesian inference.

As far as we can see, the choice between fuzzy logic and Bayesian inference is rather a personal choice, similar to the choice of a programming language: it has more consequences on the way we express our solution than on the solution itself. To extend the analogy, one might relate fuzzy logic to the C language whereas Bayesian inference would be closer to Ada.

4. Trajectory tracking with obstacle avoidance

The method presented in the previous section provides us with an efficient way to fuse a security system and orders from a high level system. Nevertheless the perturbations introduced in the trajectory following system by obstacle avoidance are such that they can make it become unstable. In this section will show how we integrate trajectory tracking and obstacle avoidance.

While following the trajectory, obstacle avoidance will modify certain commands in order to follow as much as possible desired orders while granting security. These modifications may introduce delay or diversions in the control loop. If no appropriate action is taken to manage these delays the control law may generate extremely strong accelerations or even become unstable when obstacles are gone. This is typically the case when our system evolves among moving pedestrians. Thus we designed a specific behaviour to adapt smoothly our control system to the perturbations induced by obstacle avoidance.

4.1. Multiplexed trajectory tracking

4.1.1. Validity domain of flat control law

Experimentally, we found that the control law based on flatness can manage errors in a range of about 1 m and 15° around nominal trajectory. Furthermore, as this control law controls the third derivative of the flat output (Eq. (2)), it is a massively integrating system. For this reason, a constant perturbation such as immobilisation due to a pedestrian standing in front of the vehicle will result in a quadratic increase of the control law output. This phenomenon is mainly due to the fact that when obstacle avoidance slows the robot down, it strongly breaks the dynamic rules around which the flat control law was built. So, there is no surprise in its failure.

4.1.2. Probabilistic control law

In order to deal with the situations that flat control law cannot manage, we designed a trajectory tracking behaviour (TTB) based again on probabilistic reasoning (Section 4.2). As this behaviour has many similarities with a weighted sum of proportional control laws, we do not expect it to be sufficient to stabilise the robot on its trajectory. Nevertheless, it is sufficient to bring it back in the convergence domain of the flat control law when obstacle avoidance perturbations have occurred. Basically, the resulting behaviour is as follows: while the robot is close to its nominal position, it is commanded by flat control law. When, due to obstacle avoidance, it is too far from its nominal position, TTB takes control, and try to bring it back to flat control law’s convergence domain. When it enters this domain, flat control law is reinitialised and starts accurate trajectory tracking (this is illustrated in Fig. 10).

4.1.3. Time control

Path resulting from path planning (Section 2.3) is a list of robot configuration indexed by time. So when the robot is slowed down by a traversing pedestrian, it...
compensates its delay by accelerating. Nevertheless, when the robot is stopped during a longer time, let us say 15 s, it should not consider to be delayed of 15 s, otherwise it will try to reach a position fifteen second ahead, without tracking the intermediary trajectory. To tackle this difficulty, we introduced a third mode to the trajectory tracking: when the robot comes too far from its nominal position, we freeze the nominal position, and we use the TTB to reenter the domain where nominal position can be unfrozen.

The global system is illustrated by Fig. 10: we implemented some kind of multiplexer/demultiplexer which manage transitions between control laws. In order to avoid oscillating between control laws when at the interface between two domains of validity, we had to introduce some hysteresis mechanism in the switching. This is illustrated in Fig. 10.

4.2. Trajectory tracking behaviour

Our trajectory tracking behaviour was built as a probabilistic reasoning, in a way similar to the obstacle avoidance presented above (Section 3). Functionally, it is very similar to a fuzzy control scheme as presented in [23]. If A and B are two variables, we will define a diagnosis Boolean variable $I_d$ which express a consistency between A and B. Then A and B will be called the diagnosed variables of $I_d$.

Our goal is to express the distribution over the desired controls ($V_d$, $\Phi_d$) knowing reference controls ($V_r$, $\Phi_r$) planned by the path planning stage, and error in position ($\Delta X$, $\Delta Y$) and orientation $\Delta \theta$ with respect to the nominal position. Fig. 11 illustrates these variables.

In addition to the preceding variables, we will add five diagnosis variables $I_{d1}^{X}$, $I_{d2}^{X}$, $I_{d3}^{X}$, $I_{d4}^{X}$ and $I_{d5}^{X}$. Variables linked to an error variable ($\Delta X$, $\Delta Y$, $\Delta \theta$) will diagnose if a given command helps correcting this error. Variables linked to reference commands evaluate if a command is similar to the reference one.

All these variables describe the relation between their diagnosed variables in the following joint distribution:

$$P \left( V_d \Phi_d | V_r \Phi_r, \Delta X, \Delta Y, \Delta \theta \right) = P(V_d \Phi_d | V_r \Phi_r) P(\Delta X, \Delta Y, \Delta \theta | V_r \Phi_r)$$

$$P(I_{d1}^{X} | V_r \Phi_r) P(I_{d2}^{X} | \Phi_r \Delta X) P(I_{d3}^{X} | \Phi_r \Delta Y) P(I_{d4}^{X} | \Phi_r \Delta \theta) P(I_{d5}^{X} | \Phi_r \Phi_r).$$

Using this joint distribution and Bayes rule, we will be able to infer

$$P(V_r \Phi_r | V_d \Phi_d, \Delta X, \Delta Y, \Delta \theta | I_{d1}^{X} = 1)$$

$$= \frac{P(V_r \Phi_r | V_d \Phi_d, \Delta X, \Delta Y, \Delta \theta) P(I_{d1}^{X} = 1)}{P(I_{d1}^{X} = 1)}.$$  

 Basically, this equation expresses the fact that we are looking for the most likely commands in order to correct tracking error while accounting for reference commands. Having all the diagnosis variables set to one enforces this semantic. In the preceding joint distribution (Eq. (6)), all the diagnosed variables are assumed to be independent, and to have uniform distributions. All the information concerning the relation between them will be encoded in the distribution over diagnosis variables. In order to define this distributions, we first define the function $d_{a}(x, y)$ as a Mahalanobis distance between $x$ and $y$: $d_{a}(x, y) = c^{-1/2}(x - y)^{T} \Sigma^{-1}(x - y)$. Then, for two variables $A$ and $B$, we define $P(I_{a}^{A} = 1 | A B) = d_{a}(A, B)$.
Let us see how preceding functions $S$ and $f$ are defined in specific cases.

4.2.1. Proportional compensation of errors

In the case of $H_I^X$, we set $f(X) = a \cdot X$ and $S(V_d, X) = \max((1 - \beta, b \cdot X), \sigma_{\text{max}}, \sigma_{\text{min}})$.

Expression of $f$ implies that the maximum of $P(I_{H_I^X} | V_d X)$ will be for a value of $V_d$ proportional to the error $\Delta X$. Expression of $S$ defines the constraint level associated to this speed: the bigger is the error, the more confident we are that a proportional correction will work, so the smaller is $\sigma$.

The basic behaviour resulting from this definition is that when the robot is behind its nominal position, it will move forward to reduce its error: the bigger is its error, the faster and with more confidence that this is the good control to apply.

For $H_{IV}^Y$, we use a similar proportional scheme. Its basic meaning is that when the robot has a lateral error, it has to steer, left or right, depending on the sign of this error. Again, the bigger the error, the more confident we are that we have to steer.

Finally, the same apply for $H_{IV}^\theta$, except that the steering direction depends not only of the orientation error, but also of the movement direction $V_d$.

4.2.2. Using planned controls

In the path planning stage, the trajectory was defined as a set of nominal position, associated with planned controls. The execution of the trajectory is shown in Fig. 12 and 13.
speed and steering angle. They have to be accounted for, especially when error is small.

Let us consider first $f(V_r) = V_r$ and $S(V_d, V_r) = \sigma V_r \in [\sigma_{\min}, \sigma_{\max}]$, rather close to $\sigma_{\max}$. By this way, planned speed is used as an indication to the trajectory following system. The distribution over $T_{\Theta}$ is defined using the same reasoning.

4.3. Results

Fig. 12 illustrates the basic behaviour of our trajectory tracking behaviour. In both graphs, desired command will maximise either $P(V|XV_c)$ or $P(\Phi|Y\Theta \Phi_c)$. Since curve $P(V|XV_c)$ is closer to $P(V|X)$ than to $P(V|V_c)$, we can observe that longitudinal error ($8X$) has much more influence than reference.
command on the vehicle speed. In the same manner, steering angle is a trade-off between what should be done to correct lateral error ($x$) and orientation error ($\theta$), lightly influenced by reference steering angle. Fig. 13 shows the collaboration of obstacle avoidance and trajectory following on a simulated example. Planned trajectory passes through an obstacle which was not present at map building time. Obstacle avoidance modifies controls in order to grant security. When errors with respect to nominal trajectory is too big, our control law selector switch to the trajectory tracking behaviour. Here it is a big longitudinal error, due to obstacle avoidance slowing down the vehicle, which trigger the switching.
4.4. Discussion

Using the multiplexed control laws we managed to integrate, in the same control loop, our flat control, accurate but sensible to perturbations, with our TTB, less accurate but robust to perturbations. By this way we obtained a system capable of tracking trajectory generated by our path planner while accounting for unexpected object in the environment.

Finally, when the robot has gone too far from reference trajectory, or when reactive obstacle avoidance cannot find suitable controls anymore, it may be necessary to replan a new trajectory to the goal. This has not been implemented on the robot yet, but this should not be considered neither a technical nor a scientific issue.

5. Experimental setup

We tested the integration of these essential autonomy capacities in our experimental platform the CyCab robot. The aim was to validate the theoretical considerations made for the BiS-car and to get insight into the limitations of the whole motion scheme.

The computation power on-board the CyCab is a Pentium II 233 MHz running a Linux system. All programs were written in C/C++ language.

During the experiments the speed of the robot was limited to 1.5 m s\(^{-1}\). The control rate of the robot was fixed at 50 ms. The throughput rate of the laser range-finder was limited to 140 ms;\(^5\) therefore the control system has to rely momentarily in odometry [13] readings.

Figs. 15–18 illustrate how a planned trajectory is executed while avoiding moving pedestrians. In this environment, the control law using flatness could only be used at the beginning and at the end of the trajectory. On the remaining of the trajectory, speed and steering angle are adjusted in order to maintain security while keeping pace with the plan as much as possible.

\(^5\) This rate is fair enough for our needs, even though we could use a real-time driver.
6. Discussion and conclusions

In this paper, we presented our new steps toward the autonomy of a bi-steerable car. The integration of localization, map building, trajectory planning and execution in a moderately dynamic environment was discussed. Control law using the CyCab flatness property was found to be insufficient for trajectory tracking among moving pedestrians.

Even if this integration was successful and provides satisfactory results, we are convinced that a reactive behaviour cannot be sufficient for the autonomy of a vehicle in a real urban environment. For this reason, we are working on the perception and identification of road users (pedestrians, cars, bikes or trucks). By this way, we will be able to predict future movement of “obstacles” and react accordingly, in a smarter way than the simple scheme proposed in this paper.

References


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